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A third logarithmic functional equation and Pexider generalizations (joint work with Palaniappan Kannappan)

Let $f:]0, \infty[\rightarrow \mathbb{R}$ be a real valued function on the set of positive reals. Then the functional equations:

$$\begin{aligned}f(x+y) - f(xy) &= f(1/x + 1/y) \\f(x+y) - f(x) - f(y) &= f(1/x + 1/y)\end{aligned}$$

and

$$f(xy) = f(x) + f(y)$$

are equivalent to each other.

If $f, g, h:]0, \infty[\rightarrow \mathbb{R}$ are real valued functions on the set of positive reals then

$$f(x+y) - g(xy) = h(1/x + 1/y)$$

is the Pexider generalization of

$$f(x+y) - f(xy) = f(1/x + 1/y).$$

We find the general solution to this Pexider equation.

If $f, g, h, k:]0, \infty[\rightarrow \mathbb{R}$ are real valued functions on the set of positive reals then

$$f(x+y) - g(x) - h(y) = k(1/x + 1/y)$$

is the Pexider generalization of

$$f(x+y) - f(x) - f(y) = f(1/x + 1/y).$$

We find the twice differentiable solution to this Pexider equation.