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Extended near Skolem sequences: where are we now?

Skolem-type sequences can be useful in constructing various types of designs, for example in constructing Steiner triple systems and cyclic partial triple systems.

A k-extended q-near Skolem sequence of order n is an integer sequence (s_1, \ldots, s_{2n-1}) with $s_k = 0$ such that for each $j \in \{1, 2, \ldots, n\} \setminus \{q\}$, there exists a unique i with $s_i = s_{i+j} = j$. It is straightforward to show that such a sequence exists only if

- (1) $n \equiv 0, 1 \pmod{4}$ and q and k have the same parity, or
- (2) $n \equiv 2, 3 \pmod{4}$ and q and k have opposite parity.

However, it is more difficult to show that these conditions are sufficient. We examine various families of constructions and assess what is left to do.