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Color critical hypergraphs and forbidden configurations

A k -uniform hypergraph (V, E) is 3-color-critical if it is not 2-colorable, but for every edge e the hypergraph $(V, E - e)$ is 2-colorable. Lovász proved in 1976 that

$$|E| \leq \binom{n}{k-1}$$

for a 3-color-critical k -uniform hypergraph with n vertices.

Here we give a new algebraic proof and prove a generalization that leads to a sharpening of Sauer's bound for $\text{forb}(m, F)$, where F is a k -by- ℓ 0, 1-matrix.

Joint work with R. Anstee, B. Fleming, and A. Sali.